

The dependency between annual air temperature and solar activity. A case study of Warsaw in 1951–2010.

Abstract

The paper demonstrates a dependency between the annual average daily air temperature course (cycle) in Warsaw and the profile of annual solar activity linked to rotation (with a period of 25–31 days). Waves of cold ($\Delta T < 0$) or heat ($\Delta T \ge 0$) were defined as ΔT deviations of daily average temperature (*T*) using a regression sinusoid *f*(*t*) with a period of 365 days. Cold waves were found to generally occur at times of low daily average solar activity (relative to 60-year average), while hot waves tended to coincide with high Wolf numbers. The cycles of the variables were derived using the sinusoid regression method (Boryczka 1998). The maximum sinusoid regression of the annual air-temperature cycle *T* is delayed by nearly one month vis-à-vis the maximum declination of the Sun. The waves devided from the maximum declination by more than two months.

Keywords

Cold waves $\boldsymbol{\cdot}$ heat waves $\boldsymbol{\cdot}$ solar activity $\boldsymbol{\cdot}$ regression sinusoid $\boldsymbol{\cdot}$ period $\boldsymbol{\cdot}$ interference

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Introduction

The main objective of this paper is to determine the influence of solar activity, as observed from the Earth, on the annual course of air temperatures using Warsaw over the period 1951–2010 as a case study.

In the study of the annual air temperature course a particularly important role is played by annual, or shorter, cycles of solar activity linked to the Earth's orbiting around the Sun (365.25 days) and the Sun's rotation around its axis inclined at an angle of $82^{\circ}45'$ to the plane of the ecliptic (with an inclination of the equator of $7^{\circ}15'$). The Sun has a rotation period of 25.04 days at its equator and 31 days near its poles.

The dominant contribution of solar radiation in shaping the Earth's climate during the gradual warming of the climate in the 19th to 20th century is evidenced by the synchronic changes of average air temperature in the northern hemisphere in the years 1856–2002 (Bernes, 2003) and 11-year moving average Wolf numbers (Boryczka, Stopa-Boryczka, 2004). The years 1920–2002 are characterised by significant warming, with a local minimum in the 1970s. The same is true of the deviation of the consecutive averages of Wolf numbers for the same periods. The main local minimum of the Wolf numbers corresponds to the main local minimum of the temperature in the 1970s; solar activity in the years 1925–2002 is also much greater than before 1925.

Changes in air temperature T (11-year moving average) in Europe (Paris, Berlin, Stockholm, Warsaw, Cracow, Prague, Vienna, Tallinn, Basel, Oxford) and solar activity W in the years 1840–1994 are described by regression equations (1) and (2), with correlation coefficients of r=0.913 and r=0.612, with statistical significance at <0.01 (Boryczka, 2015).

Jerzy Boryczka¹, Maria Stopa-Boryczka², Urszula Kossowska-Cezak³, Jolanta Wawer⁴

¹Institute of Physical Geography, Faculty of Geography and Regional Studies University of Warsaw, Poland *e-mail: jkborycz@uw.edu.pl*

²Institute of Physical Geography, Faculty of Geography and Regional Studies University of Warsaw, Poland *e-mail: mmstopab@uw.edu.pl*

³Institute of Physical Geography, Faculty of Geography and Regional Studies University of Warsaw, Poland

⁴Institute of Physical Geography, Faculty of Geography and Regional Studies, University of Warsaw,, Poland *e-mail: jgwawer@uw.edu.pl*

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 $T = 0.007131t - 5.16899 \tag{1}$

$$W = 0.262018 t - 445.6094 \tag{2}$$

The dependency between annual air temperature (11-year moving average) in Europe in the years 1840–1994 and solar activity is described by equation (3), with correlation coefficient of r=0.628, and statistical significance at < 0.01.

$$T = 0.01150 W + 7.86782 \tag{3}$$

The annual course of air temperature (T), represented by (60year) average daily values from continuous 365-day strings over the period 1951–2010 is illustrated by a curve with numerous peaks and troughs representing short hot and cold spells, or waves.

Examples include the cold waves in May and summer known in Poland under a variety of colourful names including, "the cold gardeners" (from patron saints Pancras, Servatius and Boniface on 12–14 May), "the cold Sophie" (patron saint of 15 May), and "the European monsoon" (June) (Kossowska-Cezak, 1994); the Indian summer hot waves known as "babie lato" (September and October); and winter warm and cold waves captured in a folk proverb "If St Barbara's (4 December) is wet then Christmas (25 December) will be icy" (Stopa-Boryczka et al., 2006).

The sources used in the study included daily air temperatures in Warsaw measured during the period 1951–2010 which were obtained from the archives of the Institute of Meteorology and Water Management. Daily values of the NAO index covering the

period 1951–2012 and daily Wolf numbers from 1951–2013 were downloaded from the on-line service at the address daily total sunspot number, dayssn import.txt.

Spectrums and cycles of air temperature (T) in Warsaw, NAO index and Wolf numbers (W) ranging from 1 to 365.25 days in length were identified using the regression sinusoid method proposed by J. Boryczka (1998).

The regression sinusoid method developed by J. Boryczka consists in adjusting the results of the y_1, \ldots, y_n measurements performed in time t_1, \ldots, t_n (using the smallest square values) of consecutive sinusoids with presumed cycles, e.g. Θ =1, 2, ..., *n* (or 0.1, 0.2, ..., *n*) according to regression sinusoid equation (4),

$$y = a_0 + b\sin\left(\frac{2\pi}{\theta}t + c\right) \tag{4}$$

where: Θ – period, *b* – amplitude, *c* – phase, *t* – time, by changing the period of sinusoid Θ every 0.1 day.

The spectrum is a sequence of the values of residual variance $\varepsilon_{1,1}^2$, ..., ε_{n}^2 corresponding to the presumed cycles Q=0.1, 0.2, ..., *n*. Periods Θ – these are local minimal values of residual variance ε^2 (local maximum values of correlation coefficient *R*) – equation (5).

$$\varepsilon^2 = \frac{1}{n} \sum_{i=1}^n \varepsilon_i^2 , \quad R = \sqrt{1 - \frac{\varepsilon^2}{s^2}}$$
(5)

where $\varepsilon_i = y_i - y(t_i)$, s^2 – variance of a variable y

The statistical significance of these cycles (i.e. multiple correlation coefficients *R*) and normal correlation coefficients *r* were assessed with the Fisher–Snedecor test $F_{calc} > F_{crit}$ (6) (Zieliński, 1972).

$$F_{\text{calc}} = \frac{n-3}{2} \frac{R^2}{(1-R^2)}$$
(6)

Interference of the identified air temperature cycles (a resultant of the cycle overlapping) was established (with a cycle of k) on the basis of the following formula (7):

$$f(t) = a_o + at + \sum_{j=1}^{\kappa} b_j \sin\left(\frac{2\pi}{\Theta_j}t + c_j\right)$$
(7)

where: t = time, and at - linear component.

Annual course of air temperature in cold and hot waves

The period's annual course of daily averages of 60-year air temperature values (*T*), minimum daily averages (*T*_{min}) and maximum daily averages (*T*_{max}) in Warsaw are described by regression sinusoids (8), (9) and (10) (with *at* – linear component, *k*=1) with a frequency of , with high multiple correlation coefficients (*R*) of 0.997, 0.979 and 0.980, and with statistical significance at < 0.01 ($F_{calc} > F_{crit}$).

$$T = f(t) = 7.6773 + 0.002239 t + +10.767682 sin ($\omega t - 1.845735$) (8)$$

$$T_{\min} = f_1 t) = -2.7659 + 0.007865 t + + 15.190194 \sin (\omega t - 1.825587)$$
(9)

$$T_{\max} = f_2(t) = 16.4562 - 0.000200 t + + 9.807196 \sin (\omega t - 1.810522)$$
(10)



Figure 1. Annual course of air temperature in Warsaw (1951– 2010): T – 60-year daily average, T_{min} – minimum daily average, T_{max} – maximum daily average, δ – angle of solar declination

The annual profiles of average daily air temperatures (T) - 60-year averages, minimum (T_{min}) and maximum (T_{max}) values in Warsaw were compared to corresponding regression sinusoids f(t), $f_1(t)$, $f_2(t)$ and to the annual solar declination cycle (δ) derived from the IW Spencer formula (1971) (Fig. 1).

The maximum values of the air temperature regression sinusoids T=f(t), $T_{\min}=f_1t$) and $T_{\max}=f_2(t)$ follow the maximum Sun declination δ_{\max} (22 June) with a nearly one-month delay:

		No	Date
δ_{max}	23.417°	173.000	22 June
Т	18.889°C	197.436	17 July
T _{min}	13.977°C	198.608	18 July
$T_{\rm max}$	26.224°C	196.561	15 July

This delay is caused by a time-shift in the daily extreme values (maximum and minimum) of the Earth's surface (ground) and the atmosphere in comparison to the upper and lower culmination of the Sun.

The annual course of the daily averages of 60-year air temperatures in Warsaw (1951-2010) depending on the daily solar declination (δ) is shown in Fig. 2a. Notably, in the second half of the year, i.e. from 22 June until the end of the year (31 December), air temperatures (upper T-curve) are considerably higher than those in the other half of the year (1 January - 22 June) (lower T-curve). The greatest air temperature difference (of more than 10°C) is observed between the spring equinox $(\delta=0^\circ, T=1.9^\circ\text{C})$ and the autumn equinox $(\delta=0^\circ, T=12.6^\circ\text{C})$. Additionally, the study presents the annual profile of the lowest 60-year values (T_{min}) and highest 60-year values (T_{max}) relative to the corresponding solar declination (δ) (Fig. 2b). The greatest difference, of 12.8°C, between the two equinoxes (δ =0) is observed at the minimum daily temperatures T_{min} (-5.5 and 7.3°C). At the other end of the spectrum, T_{max} , the difference amounts to 8.7°C (11.4 and 20.1°C).

Both cold waves ($\varepsilon_i < 0$) and heat waves ($\varepsilon_i \ge 0$) provide a good characteristic of the deviations ΔT_i (remainders ε_i) of the daily 60-year daily average values of measured air temperatures T_i from the corresponding points of the regression sinusoid *f*(*t*) with a period of Θ =365.25 days, (11a) and (11b) (Stopa-Boryczka et al., 2012; Boryczka et al., 2014) (Fig. 3).

$$T_i = f(t_i) + \varepsilon_i \tag{11a}$$



Figure 2. Annual course of air temperature in Warsaw (1951–2010) vs. angle of solar declination (δ°): a) 60-year daily average (*T*), b) 60-year minimum daily average (T_{min}) 60-year maximum daily average (T_{max})



Figure 3. Warm and cold waves in Warsaw (1951–2010), $\varepsilon_i = T_i - f(t_i) - deviation of empirical points (t_i, T_i) from sinusoid f(t) of yearly course of air temperature$

$$T_i = a_0 + bsin\left(\frac{2\pi}{365.25} t_i + c\right) + \varepsilon_i \tag{11b}$$

Earlier studies have proven that warmer and cooler spells in the annual air temperature profile (i.e. hot and cold waves) were caused by interferences between cycles lasting from single days to up to 20 days and multi-year average monthly temperature cycles (Stopa-Boryczka et al., 2006, 2011a, 2011b, 2012; Boryczka et al., 2014).

For example, cool spells in May are caused by cycles of: 6.3, 10.4 and 16.5 days summed up with the following formula (12):

 $T = 12.089 + 0.09216 t + 0.126 \sin(2\pi t/6.3 + 1.5993) + 0.290 \sin(2\pi t/10.4 - 2.2842) + 0.228 \sin(2\pi t/16.5 + 2.3874)$ (12)

that combined with multi-year average monthly temperature cycles with lengths of: 4.3, 6.1, 8.0, 18.2, 30.2 years (and with amplitudes of 0.80, 0.53, 0.28, 0.44 and 0.11°C). The most prominent cycles contributing here are: 16.5-day and 4.3-year cycles that produced the greatest differences of 0.46 and 1.6°C.

Cool spells in June (the European monsoon, Kossowska-Cezak, 1994) are caused by the overlap of cycles with a length of 7.3, 10.6 and 16.8 days (13)

 $T = 16.232 + 0.041362 t + 0.229 sin (2\pi t/7.3 + 2.9757) + 0.314 sin(2\pi t/10.6 + 2.9427) + 0.540 sin(2\pi t/16.8 - 1.3462)$ (13)

with long-term average monthly cycles with a length of 3.7, 9.0, 10.7 and 13.7 years (and with amplitudes of 0.601, 0.401, 0.319 and 0.433 °C).

The autumn waves of hot weather ("Indian summer") in September and October (on days 244-304) are caused by cycles with a duration of 15.4, 20.5 and 31.8 days (14).

$$T = 55.877 - 0.164228 t + 0.2764sin (2\pi t/15.4 - 0.9527) + + 0.1279sin (2\pi t/20.5 + 2.1943) + + 0.3160sin (2\pi t/31.8 + 2.5458)$$
(14)

combined with long-term cycles, including in September: 6.4, 7.2, 13.1, 19.9 and 38.6 years (with amplitudes of 0.611, 0.656, 0.524, 0.460 and 0.306° C) and in October: 4.8, 5.7, 7.8 and 19.2 years (with amplitudes of 0,643, 0.862, 0.515 and 0.766 $^{\circ}$ C).

It is interesting to note that the December warm and cold waves (4 December and 25 December) are caused by interference between short cycles of average daily temperature with a duration of 4.6, 7.7 and 16.8 days (and amplitudes of 0.48, 0.80 and 0.70°C), as per formula (15):

 $T = 0.575 - 0.0831 t + 0.241sin (2\pi t/4.6 + 0.0433) + 0.404sin (2\pi t/7.7 - 2.1011) + 0.350 sin(2\pi t/16.8 - 1.4969) (15)$

and long term cycles of 2.9, 6.7, 8.1,16.7 and 30.7 years (with amplitudes of 1.078, 1.348, 0.843, 1.101, 0.742) and, above all, of 6.7 and 16.7 years of average monthly air temperature (amplitudes of 2.7 and 2.2°C).

The impact of circulation on warm and cool waves

Warm and cool waves in the annual course of daily air temperatures in Warsaw during the study period were influenced by the corresponding profile of the North Atlantic Oscillation (NAO). *NAO* values indicate longitudinal movement of air masses; values above zero correspond to an eastwards movement and values below zero to a westwards movement (Marsz, 1999, 2008). A change in NAO causes short warm or cool spells of several days in length. This is demonstrated by changes in annual *NAO* values, such as the average daily (*NAO*), minimum (*NAO*_{min}) and maximum (*NAO*_{max}) values.

The annual courses of NAO, NAO_{min} and NAO_{max} are similar to regression sinusoids (16), (17), (18) of F(t), $F_1(t)$, $F_2(t)$ with the frequency , derived from 365 (366) values from successive days (of the 60-year period) (Fig. 4).

$$NAO = F(t) = -0.033666 - 0.000052 t + + 0.03856591 sin ($\omega t - 2.848821$) (16)$$

$$NAO_{\min} = F_{1}(t) = -4.085093 + 0.001626 t + + 1.931304 \sin(\omega t - 1.910102)$$
(17)

$$NAO_{max} = F_2(t) = 3.5043 - 0.000052 t + + 1.778929 sin (\omega t + 1.067360)$$
(18)

Their multiple correlation coefficients (*R*=0.207, *R*=0.466, *R*=0.345) are significant at 0.01 because the statistical values produced by the Fisher–Snedecor test (F_{calc} =8.100, F_{calc} =50.21, F_{calc} =24.45) are greater than the critical value F_{crit} =4.67.

The maximum values of NAO regression sinusoids (NAO=F(t), NAO_{min}=F1(t) and NAO_{max}=F2(t)) fall more than one month after the maximum angle of solar declination δ_{max} (173,22 VI):

NAO	-0.00544	198.787	18 VII
NAO _{min}	-1.82477	202.349	21 VII
NAO _{max}	1.736389	211.89	31 VII

The lowest average daily temperatures (T_{min}) in Warsaw in the annual profile of 1 to 365.25 days (1951–2010) are strongly correlated with the lowest NAO values (NAO_{min} , r=0.899) while the highest daily averages (T_{max}) display a similar correlation with the highest NAO values ($NAO_{max'}$, r=-0.858).

Both the ranges of the lowest average daily temperature (T_{min}) in Warsaw and the lowest NAO_{min} values feature cycles of nearly identical lengths, i.e. 151.8 and 152.6 days long, with amplitudes of 11.84°C and 1.644°C respectively, and correlation coefficients of R=0.453 and R=0.491 that are statistically significant at 0.01 (F_{calc} =46.733 and F_{calc} =57.497, and F_{crit} =4.67).



Figure 4. Annual course of the NAO (1951–2010), NAO – daily average, NAO_{min} – minimum and NAO_{max} – maximum

Similarly, the ranges of the highest daily temperature T_{max} and the highest NAO_{max} feature similar cycles of 146.2 and 150.4 days in length and amplitudes of 6.03°C and 1.08°C correlated at R=0.340 and R=0.428, significant at 0.01 ($F_{calc}=23.66$, $F_{calc}=40.59$).

Typically, when NAO values were significantly above zero Warsaw experienced a warm wave ($eT \ge a$ lues were sNAO was lower than zero it experienced a wave of cool weather (rT < 0) (Fig. 5).

The influence of solar activity on warm and cool waves

The range of the average daily Wolf numbers (*W*) during the study period (Fig. 6) features cycles with durations Θ , amplitudes *b* and phases *c*, where *R* is the correlation coefficient and *F*_{calc} represents the Fisher–Snedecor test (Tab.1). In the range of daily maximum Wolf numbers (W_{max}) the longest cycles equal Θ =122 days and 365.25 days.

The annual profile of Wolf numbers, including daily average W (1951–2013) and the daily maximum W_{max} (1951–2010), is well matched by regression sinusoid formulae of assumed frequency (19) and (20).

 $W = 66.832 + 0.00466 t + 1.776792 \sin(\omega t - 2.431845)$ (19)

$$W_{m} = 237.2007 + 0.037789 t + 12.604851 sin(\omega t - 2.737850 (20))$$

Correlation coefficients R=0.433 and R=0.385 are significant at 0.01 (Fisher–Snedecor test F_{calc} =41.65 and F_{calc} =29.059 are greater than F_{crit} =4.67).

The maximum of the regression sinusoid of daily average Wolf numbers *W* (1951–2013) was delayed from the maximum angle of solar declination δ_{max} (173, 22 June) by more than two months (20 August) and the maximum of the sinusoid of the highest daily Wolf numbers W_{max} (1951–2010) is delayed by nearly 3 months (7 IX) (Fig. 7):

W	69.69308	232.679	20 VIII
W _{max}	259.2705	250.468	7 IX

It is important to note that in the annual cycle caused by the Earth orbiting around the Sun, the increase in the daily average temperature T between January and mid-July may is also caused by the increase in solar activity (daily Wolf numbers W) and its subsequent decrease until December may also be caused by a drop in solar activity W (Fig. 8).



Figure 5. Warm waves ($\Delta T \ge 0$) and cool waves ($\Delta T < 0$) in Warsaw vs. average annual course of daily NAO (1951–2010)



Figure 6. Spectrum of daily Wolf numbers W (1951–2013)

Table 1. Cycles of daily average Wolf numbers (1951-2013)

Θ days	b	с	R	F _{calc}
28.5	1.574105	1.952977	0.307	13.62
52.3	1.48891	-2.644511	0.339	17.02
68.7	1.236791	-0.652153	0.269	10.21
137.8	0.662988	2.517657	0.178	4.29
365.25	1.798819	-2.545154	0.425	28.84

This delay in the daily extremes (maximums and minimums) of air temperature relative to the upper and lower culmination of the Sun is not just caused by the physical process of heat energy exchange between the active surface (ground) and the atmosphere, but also by the annual profile of the Sun's activity (numbers of spots visible from the Earth on the face of the rotating Sun).

The annual change in the deviations (ΔT) of the average daily air temperatures $\varepsilon_i = T_i - f(t_i)$ and of the daily Wolf numbers (*W*) tend to be synchronous (Fig. 9). There is also a coincidence of the extremes in the annual deviations of the highest average daily temperatures $\Delta T_{max} = T - f_2(t)$ and the maximums of the Wolf numbers (W_{max}) (Fig. 10).

To demonstrate a high dependence of the annual air temperature course in Warsaw on Wolf numbers during the study period, a comparison was made between the regression sinusoids with the longest periods occurring in the oscillation ranges (except the annual cycles Θ =365.25 days): *T*=147.9 days, *W*=137.8 days (1951–2013), *T*_{min}=151.8 days, *T*_{max}=146.2 days and *W*_{max}=122.0 days. These cycles have significant multiple correlation coefficients (*R*), respectively of 0.386, 0.283, 0.453, 0.340 and 0.384 (*F*_{0.01}=4.67), equations (21), (22), (23), (24) and (25).



Figure 7. Annual course of air temperature in Warsaw (1951–2010) and of solar activity (Wolf numbers), a) T and W, b) T_{max} and W_{max}



Figure 8. Dependence of air temperature in Warsaw (1951–2010) on solar activity (Wolf numbers), a) T on W, b) T_{max} on W_{max}



Figure 9. Warm and cool waves $\varepsilon_i = T_i - f(t_i)$ in Warsaw vs. Wolf numbers (W) (1951–2010)



Figure 10. Warm and cool waves $\Delta T_{max} = T_{max} - f_2(t)$ in Warsaw vs. maximum daily Wolf numbers (W_{max}) (1951–2010)



Figure 11. Annual change in air temperature in Warsaw and in Wolf numbers (1951–2010): a) daily averages (T, W); b) minimum (T_{min}) and maximum (T_{max}) annual daily air temperatures and W_{max}

	R	F _{calc}	
$T = 5.4431 + 0.016665t + 3.419359sin (2\pi t/147.9+3.064770)$	0.386	31.49	(21)
$T_{\min} = -5.4719 + 0.026545t + 5.929996sin (2\pi t/151.8 - 2.916341)$	0.453	46.73	(22)
T_{max} = 14.6991 + 0.011321 <i>t</i> + 3.017739sin (2 π <i>t</i> /146.2 + 2.916286)	0.340	23.66	(23)
	R	F_{calc}	
W = 65.5772 + 0.012035 t + 1.038030sin (2πt/137.8 + 2.224552)	0.385	31.40	(24)
W_{max} = 225.7675 + 0.100149 <i>t</i> + 8.766014sin (2 π <i>t</i> /122.0 +1.430669)	0.384	31.31	(25)

There is also a noteworthy coincidence of the extremes and a trend towards an increase in the average daily air temperature (*T*) in Warsaw with a cycle of 147.9 days and in the average daily Wolf numbers (*W*) with the cycle of 137.8 days (1951–2013) (Fig.11a). A similar conclusion about the lowest (T_{min}) and highest (T_{max}) daily air temperatures in Warsaw being dependent on maximum daily Wolf numbers (W_{max}) can be drawn from a comparison of sinusoids with the periods T_{min} =151.8 days, T_{max} =146.2 days and W_{max} =122.0 days (Fig.11b).

Other indications of the dependence of the climate on solar activity include, for example, synchronic fluctuations of average 11-year moving Wolf numbers (W) (correlation coefficient r=0.397 significant at the 0.01 level) and the width (d) of *Picea abies* spruce tree rings at Stonnglandes (Norway, 1403–1997) (Fig.12).

Other indications of the dependence of the climate on solar activity include, for example, synchronic fluctuations of average 11-year moving Wolf numbers (*W*) and the width (*d*) of 5 trees growing in Europe: *Pinus silvestris* (Fortfjorddalen, Norway, 877–1994), *Picea abies* (Falkenstein, Germany, 1540–1995), Fodara Vedla (Italy, 1598–1990), Stonnglandes (Norway, 1403–1997) and *Larix deciduas* (Pinega, Russia, 1578–1990) (correlation coefficient r=0.236 significant at the 0.01 level) (Fig. 13).

Conclusions

The annual courses of average daily air temperatures (*T*) – 60-year averages, minimum (T_{min}) and maximum (T_{max}) values in Warsaw were compared to corresponding regression sinusoids *f* (*t*), and to the annual solar declination cycle (δ).

The maximum values of the air temperature regression sinusoids *T* (17 July), T_{min} (18 July) and T_{max} (15 July) follow the



Figure 12. Synchronous fluctuation of the width of spruce tree rings (Picea abies) at Stonnglandes (1403–1997, Norway) and Wolf numbers (1700–1997) (11-year moving averages), correlation coefficient r=0.397



Figure 13. Synchronous fluctuations of average tree ring widths of 5 of trees growing in Europe and Wolf numbers in the years 1700–2015 (11-year moving average), correlation coefficient r=0.236

maximum Sun declination $\delta_{max} = 23.4^{\circ}$ (22 June) with a nearly one-month delay. The maximum values of *NAO* regression sinusoid (18 July) fall more than one month after the maximum angle of solar declination δ_{max} . The maximum of the regression sinusoid of daily average Wolf numbers *W* (1951–2013) was delayed from the maximum angle of solar declination δ_{max} by more than two months (20 August).

Notably, in the second half of the year, i.e. from 22 June until the end of the year (31 December), air temperatures are considerably higher than those in the other half of the year (1 January – 22 June).

The increase in the average daily air temperature T observed between January and mid-July is caused not only by an increase in the angle of the Sun's declination, but also by an increase in solar activity (Wolf number W), while the subsequent decrease in temperature lasting until December is also caused by the falling W numbers.

This delay in the daily extremes (maximums and minimums) of air temperature relative to the upper and lower culmination of the Sun is not only caused by the physical process of heat energy exchange between the active surface (ground) and the atmosphere, but also by the annual profile of the Sun's activity (numbers of spots visible from the Earth on the face of the rotating Sun).

Both cold waves ($\varepsilon_i < 0$) and heat waves ($\varepsilon_i \ge 0$) provide a good characteristic of the deviations ε_i of the daily 60-year daily average values of measured air temperatures T_i from the corresponding points of the regression sinusoid formula $f(t_i)$ with a period of Θ =365.25 days.

Cold waves were found to generally occur at times of low daily average solar activity (60-year), while hot waves tended to coincide with high Wolf numbers. There is also a coincidence of the extremes of shorter air temperature cycles of Θ =147.9 days and Wolf numbers of Θ =137.2 days.

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